

A High-Accuracy and High-Speed 2-D 8x8 Discrete Cosine Transform Design

Trang T.T. Do, Binh P. Nguyen

Department of Electrical and Computer Engineering
National University of Singapore, Singapore 117576
{dothutrang, phubinh}@nus.edu.sg

Abstract— In this paper, a high-accuracy and high-speed 2-D 8x8 Discrete Cosine Transform (DCT) design is proposed. By using the parallel architecture, inherited from the design reported by S. Ramachandran et. al., re-designing and enhancing function of all component modules, the proposed design can transform each 8x8 block in 64 cycles and achieve a very high accuracy compared to other designs and standard references. The proposed design implemented on Xilinx Virtex 4 can run at the speed of 308 MHz, processing images of size 1920 x 1080 pixels at the rate of 145 frames per second.

Keywords- DCT, Discrete Cosine Transform, Pipeline, FPGA, Parallel Matrix Multiplication, Parallel Architecture.

I. INTRODUCTION

The Two Dimensional Discrete Cosine Transform (2-D DCT) is used as a transform coding scheme in most video standards such as HDTV video coding, JPEG and MPEG. Since DCT requires a highly intensive computation, different efficient DCT algorithms have been reported. There have also been numerous efforts to efficiently map and implement these algorithms into VLSI chips. In the literature, some hardware designs have a very high speed but low accuracy, while some other designs have a good accuracy but running at a low speed. Therefore, an efficient design running at a high speed and having a high accuracy is needed.

Among the high-speed group, the DCT processor in [1]-[3] is one of the fastest designs. It is implemented based on a parallel matrix multiplication algorithm and a parallel architecture. However, it is not as accurate as standard references such as Matlab (after rounding), and Xdiv MPEG 4.

Inherited from this parallel architecture, a high-accuracy and high-speed DCT design, which can transform each 8x8 image block in 64 cycles, is proposed. By efficiently re-designing all modules, the proposed design has a significant improvement in terms of accuracy while still maintaining the high speed compared to the original architecture and other designs.

The remaining of the paper is organized as follows. The parallel algorithm in [1]-[3] is represented in Section II. The design of the DCT module is proposed in Section III, followed by the Simulation Results and Discussion in Section IV. The paper ends with Conclusion in Section V.

II. PARALLEL MATRIX MULTIPLICATION ALGORITHM FOR DCT

2D-DCT for an 8x8 pixels block of a digital image is defined as:

$$DCT(u,v) = \frac{1}{4}c(u)c(v) \sum_{x=0}^7 \sum_{y=0}^7 f(x,y) \left[\cos \frac{(2x+1)u\pi}{16} \right] \left[\cos \frac{(2y+1)v\pi}{16} \right] \quad (1)$$

where

$f(x,y)$ is the pixel intensity

$$c(u) = c(v) = \frac{1}{\sqrt{2}} \quad \text{for } u = v = 0 \quad \text{and} \quad (2)$$

$$= 1 \quad \text{for } u, v \in [1,7]$$

The 2-D DCT can be conveniently expressed in a matrix form:

$$DCT = CXC^T \quad (3)$$

where X is the input image matrix, C and C^T are the cosine coefficient matrix and its transpose with constants $\frac{1}{2}c(u)$ and $\frac{1}{2}c(v)$ absorbed in C and C^T respectively.

An expanded form of (3) is as followed:

$$DCT = \begin{bmatrix} c_{00} & c_{01} & \dots & c_{07} \\ c_{10} & c_{11} & \dots & c_{17} \\ \vdots & \vdots & \vdots & \vdots \\ c_{70} & c_{71} & \dots & c_{77} \end{bmatrix} \begin{bmatrix} x_{00} & x_{01} & \dots & x_{07} \\ x_{10} & x_{11} & \dots & x_{17} \\ \vdots & \vdots & \vdots & \vdots \\ x_{70} & x_{71} & \dots & x_{77} \end{bmatrix} \begin{bmatrix} c_{00} & c_{10} & \dots & c_{70} \\ c_{01} & c_{11} & \dots & c_{71} \\ \vdots & \vdots & \vdots & \vdots \\ c_{07} & c_{17} & \dots & c_{77} \end{bmatrix} \quad (4)$$

$$DCT = \begin{bmatrix} p_{00} & p_{01} & \dots & p_{07} \\ p_{10} & p_{11} & \dots & p_{17} \\ \vdots & \vdots & \vdots & \vdots \\ p_{70} & p_{71} & \dots & p_{77} \end{bmatrix} \begin{bmatrix} c_{00} & c_{10} & \dots & c_{70} \\ c_{01} & c_{11} & \dots & c_{71} \\ \vdots & \vdots & \vdots & \vdots \\ c_{07} & c_{17} & \dots & c_{77} \end{bmatrix} \quad (5)$$

$$DCT = \begin{bmatrix} \sum_{i=0}^7 p_{0i}c_{0i} & \sum_{i=0}^7 p_{0i}c_{1i} & \dots & \sum_{i=0}^7 p_{0i}c_{7i} \\ \sum_{i=0}^7 p_{1i}c_{0i} & \sum_{i=0}^7 p_{1i}c_{1i} & \dots & \sum_{i=0}^7 p_{1i}c_{7i} \\ \vdots & \vdots & \vdots & \vdots \\ \sum_{i=0}^7 p_{7i}c_{0i} & \sum_{i=0}^7 p_{7i}c_{1i} & \dots & \sum_{i=0}^7 p_{7i}c_{7i} \end{bmatrix} \quad (6)$$

where

$$p_{ik} = \sum_{j=0}^7 p_{ji}c_{jk} \quad (7)$$

Equation (3) can be implemented by parallel architecture wherein eight partial products (row vectors of

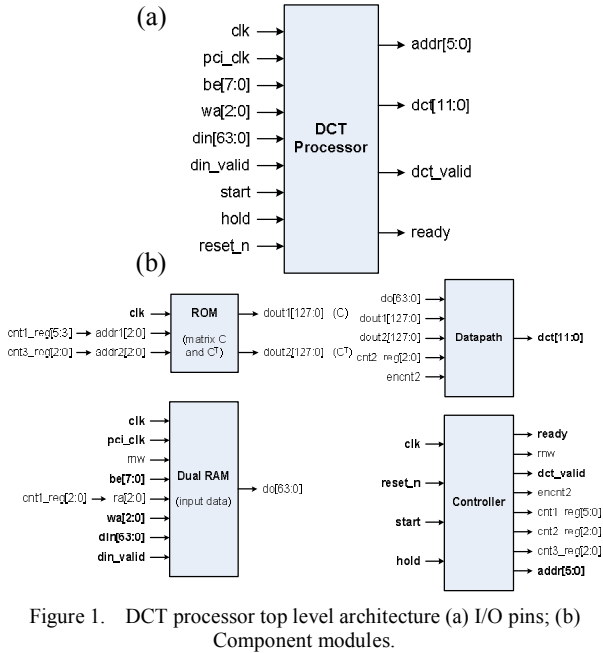


Figure 1. DCT processor top level architecture (a) I/O pins; (b) Component modules.

matrix CX) generated in the first stage are fed to the second stage in a pipeline. Subsequently, eight row vectors of CX are multiplied by the C^T matrix to generate eight DCT coefficients which correspond to a row of CXC^T . While computing the $(i+1)^{th}$ partial products of CX , the i^{th} row DCT coefficients can also be computed simultaneously since the i^{th} partial products of CX are already available.

III. THE PROPOSED DCT PROCESSOR

A. DCT Core Top Level

The proposed DCT processor architecture is inherited from the parallel architecture of [1]-[3], which includes a controller, a datapath, a ROM and a RAM (Fig. 1). All the modules are re-designed with enhanced function to increase the accuracy.

The input/output pin system of DCT processor is shown in Fig. 1a. Any image block (8 x 8 pixels) can be input as one row of a block, i.e., 8 pixels at a time; via a 64-bit bus. The DCT processor takes 64 clock cycles to process one block of image. Assuming that the input bus clock, “pci_clk”, and the DCT clock, “clk”, are the same, the host has enough free time (56 clock cycles) to attend to other processing cores. The data input bus is denoted as “di[63:0]”. Further, be[7:0] is used to identify which bytes in “di” are enabled. Also, it is necessary to have 3 bits of write address, “wa[2:0]”, for writing eight rows of a block of data. All these activities must be synchronous to the clock signal, “pci_clk”. When the data input, “di”, is valid, the DCT engine is informed by a signal “din_valid”. Besides, an asynchronous, active low signal, “reset_n” is used to reset the system. The description of DCT core signal can be seen in Table I.

B. Sequence of Operations

The operation sequences of the host processor and the DCT processor are as follows:

For the host:

1. Assert “reset_n” signal to initialize the DCT processor.

TABLE I. DCT CORE SIGNAL DESCRIPTIONS

Signal	IN/OUT	Description
clk	Input	DCT system clock.
pci_clk	Input	Bus clock used to transfer data to DCT system.
be[7:0]	Input	Byte enable active low signal, be[0] selects di[7:0] and so on.
wa[2:0]	Input	This furnishes the row address of an image block. wa[0] is the first row.
din[63:0]	Input	For each row of an input image block, di[7:0] is the first pixel and di[63:56] is the last in the row. A pixel is of size 8 bits, unsigned.
din_valid	Input	This input signals when the input data, di[63:0], is valid.
start	Input	Active high starts and maintains the DCT processing.
hold	Input	DCT processing can be kept on hold. De-asserting resumes the processing without any latency.
reset_n	Input	Asynchronous, active low.
ready	Output	Indicates the ready status to accept image input block of the core.
dct_valid	Output	Indicates the validity of DCT coefficient.
addr[5:0]	Output	DCT coefficient address
dct[11:0]	Output	DCT output in 2-complement

2. After ascertaining that “ready” signal is set by DCT processor, write an image block of 8 x 8 pixels into one block of the 64-byte Dual RAM in the DCT core via the data bus “di[63:0]”, 8 bytes each time. During this data input duration, “din_valid” is asserted as well. Besides, the “be” bits may be simultaneously asserted.
3. Issue “start” signal to begin DCT processing. This signal must be continuously asserted for continuous processing.
4. Wait for the set “ready” signal. Then write the next image block into another block of 64-byte Dual RAM in the DCT core.

Note: Normally, the host processor asserts “reset_n” signal once at the beginning of the DCT processing. However, it may apply “reset_n” anytime to terminate the current processing.

For the DCT processor:

1. If “reset_n” is active, the core will terminate the current processing and initialize all internal registers. One bank of the 64-byte Dual RAM is in write-only mode for the host to write the image block into, while the other is in read-only mode for the DCT processing. Set the “ready” signal to inform the host about its ready status.
2. Wait for the asserted “start” signal to begin the processing. Assert “ready” signal for the host to write image data into the other Dual RAM bank concurrently. After being computed, the DCT coefficients are issued at dct[11:0] pins, valid at the positive edge of “clk” with “dct_valid” signal asserted after a latency of 37 cycles. “dct_valid” signal is continuously asserted as long as the processing continues without a break. “addr[5:0] is valid upon the DCT is valid. This step is continuously processed as long as “start” is kept asserted and “reset_n” or “hold” is not active.

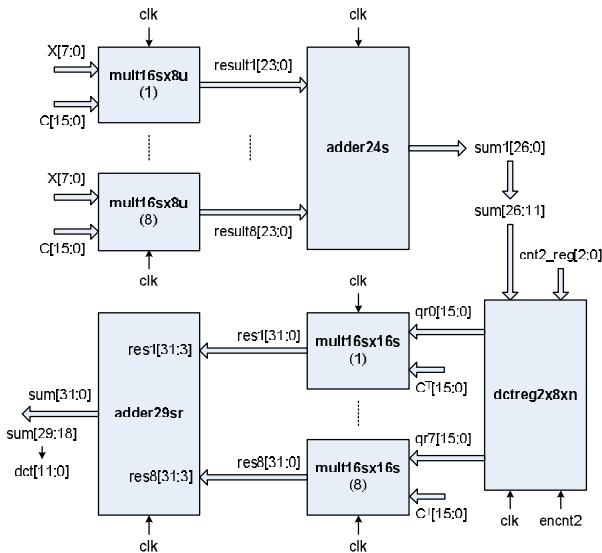


Figure 2. Datapath module

C. Modules Description

The overview of modules inside the DCT core is shown in Fig. 1b.

1) Dual RAM

The Dual RAM consists of two RAMs, each of which stores the image data written from a host processor. Actually, these two RAMs store the X matrix in the algorithm described in Section II. Initially, one of the two RAMs is filled and once it is full, the image data is written to the second RAM. While the second RAM is being written into, the first one will be read concurrently for calculating DCT coefficients.

The signal named “din_valid” is used to signal the validity of the input data signals, “di [63:0]”. Likewise, the “be[7:0]” pins are used to indicate the validity of each of the 8 bits in the 64 bit data bus. For writing one pixel block, we need 3 bits address, wa[2:0], corresponding to eight 64-bits-width locations. Image data is written at the positive edge of “pci_clk” signal. The signal, “rnw”, meaning read negative (low) and write positive (high), is used to configure one of the two RAMs in write mode while the other is in read mode. The RAM is written row-wise and read column-wise. This is due to the fact that the X matrix is accessed by column when computing the matrix multiplication CX. “ra[2:0]” is the read address to transfer the column-wise data to the output, “do[63:0]” at the rising edge of “clk”.

2) ROM

The next module is a ROM storing $2C$ and $2C^T$ matrices. These two matrices are used instead of C and C^T for accuracy improvement. Then, the final result will be divided by two in order to get the correct value for DCT. Because the cosine coefficients were stored under the 16-bit signed format (i.e. they have one significant bit and 15 bits after the decimal point), the final results will be more accurate than the result of [3] which uses only 13 bits fixed point fraction. C and C^T are row-wise simultaneously accessed through “dout1[127:0]” and “dout2[127:0]” when computing DCT coefficients. The matrices content in “dout1[127:0]” and “dout2[127:0]” are in 2-complement. “addr1” and “addr2” inputs are used for fetching C and C^T matrices. Actually, “addr1” and “addr2” inputs are respectively “cnt1_reg[5:3]” and

“cnt3_reg[2:0]”, which are sent from Controller module. C is used in the first stage multiplication, while C^T is used in the second stage multiplication.

3) Datapath

In this module (Fig. 2), eight multipliers, “mult16sx8u”, accomplish the computation of CX , where X is the unsigned input and C is the signed cosine term. These results are in 2-complement. The next module, “adder24s” is used for adding 24-bit partial products of CX (result1–result8). After being cut off the last 11 bits, the result, “sum1” is stored in “dctreg2x8xn” registers, which contains eight numbers of 16-bit registers, qr0–qr7. In order to compute $(CX)C^T$, each row of partial products of CX is stored in these registers and will be preserved for the next eight “clk” cycles. In the second stage, the partial products, qr0–qr7 are taken to multiply with the corresponding column elements of C^T for producing independent multiplied 32-bit results “res1”–“res8”. The eight multipliers, “mult16sx16s”, are used to accomplish this. Note that the bit precision has increased. “dout2” of ROM module is the C^T output, fed as one of the inputs to these multipliers. These results, “res1” through “res8”, are added together by “adder29sr” module. Note that we retain only the most significant 29 bits for each input of this adder. The sum, naturally, is 18 bits more. The least significant 18 bits and the most significant 2 bits of the result are truncated, retaining only 12 bits. It is a DCT coefficient.

4) Controller

This module generates all the control and handshake signals required for other modules to compute DCT coefficients. There are four counters, “cnt1_reg”, “cnt2_reg”, “cnt3_reg” and “addr” in the controller design. The first three counters are the pipeline registers and counter “addr” serves as the address (index) of the DCT coefficients. The enable signals of the four counters, “encnt1” to “encnt4” are realized by four “always” sequential blocks in Verilog. Note that all the “always” sequential blocks have their respective signals initialized when system reset “reset_n” is applied and the signals’ value are frozen so long as “hold” signal is asserted. The first counter is enabled right at the beginning when the user asserts the “start” signal (after reset signal is withdrawn) to commence the DCT computation. And it is disabled when DCT engine completes processing the last coefficient of a block. The enable signals, “encnt2” to “encnt4”, are activated when the first counter “cnt1_reg” is respectively 14, 20 and 36 in order to allow the counters “cnt2_reg”, “cnt3_reg” and “addr” to start running at the appropriate time. “cnt1_reg” to “cnt3_reg” serve as the read addresses for the modules, “dualram”, “romc” and “dctreg2x8xn”, and “addr” serves as the address of the DCT coefficients.

IV. SIMULATION RESULTS AND DISCUSSION

The proposed design can be implemented on FPGAs or ASICs. In simulation phase, a single Xilinx FPGA device, XC4VLX25-12SF363 was used. The simulation shows that the latency between input and output of this DCR core is 37 cycles. Once the pipeline (37-depth) is full, the DCT coefficients can be issued one every clock cycle without a break. It takes 101 cycles totally to process the first image block. However, since the second block onward, as long as the “start” signal is kept asserted and “reset_n” or “hold” is not active, it will take only 64

TABLE II. DEVICE UTILIZATION SUMMARY COMPARISON BETWEEN THE PROPOSED DESIGN AND DESIGN IN [1]-[3]

Logic Utilization	Used	Avail.	Utilization (proposed)	Utilization ([1]-[3])
Number of Slices	7260	10752	67%	38%
Number of Slice FFs	9644	21504	44%	25%
Number of 4 input LUTs	11194	21504	52%	25%
Number of bonded IOs	101	240	42%	22%
Number of GCLKs	2	32	6%	6%

TABLE III. TIMING SUMMARY COMPARISON

Feature	Proposed	[1]-[3]
Minimum period (ns)	3.245	2.930
Maximum Frequency (MHz)	308.182	341.239
Minimum input arrival time before clock (ns)	4.760	4.766
Maximum output required time after clock (ns)	3.820	3.820

TABLE IV. COMPARISON OF DCT RESULT (FIRST 16 DCT COEFFICIENTS)

Matlab (original)	Matlab (rounded)	Proposed design	[1]-[3]	Xdiv MPEG-4
547.6250	548	548	550	548
29.1097	29	29	28	29
-8.6792	-9	-9	-9	-9
-2.3442	-2	-2	-3	-2
-2.8750	-3	-3	-4	-3
-2.2495	-2	-2	-4	-2
-1.6816	-2	-2	-3	-2
-1.2775	-1	-1	-2	-1
66.2014	66	66	64	66
43.4818	43	43	43	44
-13.5491	-14	-14	-14	-14
-3.8944	-4	-4	-4	-4
-5.5206	-6	-6	-7	-5
-3.3795	-3	-3	-4	-3
-2.5010	-3	-3	-4	-2
-0.7370	-1	-1	-2	-1

cycles for processing each image block. This also can be derived from the architecture and the operation of the DCT core.

In this FPGA implementation, the maximum frequency achieved is 308 MHz (Table 3), meaning that each cycle equals to 3.3 ns. DCT computation for an 8 x 8 pixel block requires 64 clock cycles, that is, 212 ns. Therefore, for a HDTV 1920 x 1080 pixel image frame (32400 blocks), the processing time will be approximately 6.9 ms (32400 x 212 ns). Hence, it is capable of processing images of size 1920 x 1080 pixels at the rate of 145 frames per second.

In order to compare the simulation results with the original design, another DCT core architecture extracted from the DCTQ processor design in [3] was implemented as well. The synthesis results of the two designs can be summarized in Table II and Table III.

While the new design appears to be more resource demanding compared to the original design, it does not pose any implementation problem. In fact, the remaining resource is more than sufficient to implement cores like quantization and Huffman coding. As for the throughput, both the two designs provide extremely high speed performance and capable of real-time operations. The key advantage in the new design is its accuracy. Several tests are carried out, showing that the original architecture's results deviate from Matlab computed values. The same tests on the new architecture produce DCT coefficients that are the same as that calculated by Matlab. Table 4 compares the first 16 DCT coefficients of an image block produced by the Matlab, the new design, the original design, and a 2-D DCT implementation of [4], which was used in the source code of Xvid MPEG-4 Video Codec. All bold values are different from the Matlab values after being rounded.

In this DCT processor architecture, while the input data is read by block, the output DCT coefficients are produced serially. This may slow down the processing speed of the next component. However, this problem can easily be solved by adding one Dual RAM module to the design. This RAM will be used as a buffer for storing the DCT coefficients.

V. CONCLUSIONS

Based on the reported parallel architecture [1]-[3], the proposed design with the enhancement in all component modules can transform each 8x8 block in 64 cycles and achieve a very high accuracy while maintaining the speed. The proposed design can run at the maximum speed of 308 MHz on Xilinx Virtex 4 platform, processing images of size 1920 x 1080 pixels at the rate of 145 frames per second, which meets the real-time requirements for high definition. Moreover, this architecture has a great potential in practical since the matrix multiplication form CXC^T is frequently used in numerous problems.

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